

MDC High School Mathematics Competition 2010
Miami Dade College Wolfson Campus

Team Competition

Problem #1

Find all values of the number k for which the system

$$\begin{cases} x^2 + y^2 = 1 \\ y = k(x - 2) \end{cases}$$

has exactly one solution.

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Problem # 2

Find all solutions to the following trigonometric equation

$$4 \sin(2x) + 3 \cos(2x) = 5$$

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Problem # 3

Find all functions $f(x)$ such that $f\left(\frac{x-1}{x+1}\right) = x^2$

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Problem # 4

Find all possible real values of the number c for which is true that

$$0 < \frac{1}{x^2 + x + c} \leq 2$$

for all real values of x .

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Problem # 5

Find all solutions to the following trigonometric equation

$$\cos^2\left(\frac{7x}{2} - \frac{\pi}{4}\right) + \cos^2 x = 0$$

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Problem # 6

Find all possible real values of the number k for which the equation

$$\frac{x}{x^2 + 1} = k$$

has at least one real solution.

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Problem # 7

A mother plans to distribute her estate, worth \$400000 between her four sons as follows: $\frac{1}{4}$ of the estate is to be split equally among the sons. For the rest, each son is to receive \$3000 for each year that remains until his 40th birthday. Given that the sons are all 4 years apart, how much would each receive from their mother's estate?
(Hint: Let "x", "y", "z" and "w" be the amount of money that each son will receive from the splitting of $\frac{3}{4}$ of the estate according to age, starting with the oldest one.)

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Problem # 8

Find all solutions to the following trigonometric equation.

$$(1 - \tan x)(1 + \sin(2x)) = 1 + \tan x$$